

Effects of Temperature and Moisture Gradients on Slab Deformation for JPCPs

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Abstract: Slab curvature, which represents the response of concrete pavement slabs to environmental loads, influences the location and magnitude of critical slab stresses and affects long-term pavement performance. The purpose of this study was to measure the changes in temperature and moisture profiles in a newly constructed concrete pavement and to determine both the overall deformed shapes of the slabs as well as the relative contributions of built-in and transient environmental effects over time. Data were collected from an instrumented jointed plain concrete pavement (JPCP) over a two-year period. Slab curvatures were computed or predicted using measurements of temperature and moisture conditions in the slab, static strain measurements, and pavement surface profile measurements. It was found that the additional restraint provided by the dowel and tie bars does not appear to significantly reduce slab curvature resulting from daily temperature fluctuations or from reversible drying shrinkage. It does have a substantial effect on reducing slab curvature due to long-term drying shrinkage. It was also found that the Mechanistic-Empirical Pavement Design Guide default value is close to that measured in this study for the restrained slab but does not appear to be appropriate for unrestrained (i.e., undoweled) slabs.

CE Database subject headings: Concrete Pavement, Curling, Warping, Slab Curvature, Drying shrinkage.

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1.0 Introduction

It is generally assumed that transverse slab cracking in jointed plain concrete pavements (JPCP) initiates at the bottom of the slab near midpanel. There is now evidence that the fatigue cracks can, and typically do, initiate at the top of the slab and propagate downward (ARA 2004; Gutierrez 2008; McCracken et al. 2008). This is believed to be due to the combined effects of environmental loading (i.e., temperature and moisture gradients that cause slab deformation) and axle loading.

Jointed plain concrete pavements (JPCP) are usually subjected to a wide range of temperature and moisture conditions throughout their service lives, resulting in a correspondingly broad range of deformed slab shapes. Recognizing that the shape of the slab at the time of traffic loading significantly affects the development of slab stresses, the mechanistic-empirical pavement design guide (MEPDG) considers environmental effects in the computation of the critical stresses for top-down and bottom-up cracking and determines accumulated damage for each possible failure mode (i.e., top-down or bottom-up cracking) individually (ARA, 2004). For this reason, the shape of the slab must be accurately characterized for input to the MEPDG in order to produce the most accurate predictions of cracking and JPCP service life.

Slab curvature, which varies primarily with transient slab temperature and moisture conditions, is also influenced by several additional factors including: (1) temperature and moisture conditions at the time of construction (i.e., “built-in gradients”, which affect the long-term behavior of the slab); (2) concrete material properties, such as the coefficient of thermal expansion, drying shrinkage, creep and elastic modulus of the concrete; (3) restraints to slab deformation, such as slab self-weight, friction at the slab/subbase interface and restraints to joint movement (e.g., dowel bars, tie bars and aggregate interlock) (ARA, 2004). The first of these factors, built-in gradients, is the primary focus of this paper.

Temperature and moisture gradients at the time of set greatly affect slab curling and warping. The effective built-in temperature gradient is defined as the effective gradient due to combined effects of temperature and moisture gradients that are present in the slab when it sets as well as the long-term irreversible drying shrinkage. The time of set is when the concrete behavior changes from plastic to elastic, and is when the concrete can begin to carry structural stresses and strains. The actual value of the effective built-in temperature gradient is dependent on factors such as the coefficient of thermal expansion/contraction of the PCC mix, temperature conditions at the time of paving, and curing practices and conditions. Prior to the time the concrete sets, the slab remains flat because the concrete is in a plastic state. After the concrete sets, the response of the slab is affected by the magnitude and direction of the effective built-in temperature gradient. For example, when the slab temperature is uniform (i.e., no temperature gradient exists), it may be curled rather than flat because it can only be flat when the transient gradient equals the built-in gradient (after adjusting for any creep or relaxation effects that have developed over time). The curling is upward if the built-

in gradient is positive and downward if it is negative. The built-in construction gradient has proven to be an important factor in estimating stress in concrete pavements, especially when using the MEPDG (Hansen et al., 2006; Wells et al., 2006; Yu et al., 1998; Yu and Khazanovich, 2001; Ruiz et al., 2001; Rao and Roesler 2005; Eisenmann and Leykauf, 1990).

This paper examines three different approaches to determining the curvature of in-service JPCP panels in the presence of measured temperature and moisture conditions: use of slab temperature and moisture measurements, strain gage measurements and surface profile measurements. These three methods are applied to data collected from an instrumented JPCP and are used to evaluate the effects of built-in gradients (drying shrinkage) on slab curvature.

2.0 Project Description

This research effort was focused on characterizing the temperature and moisture conditions to which an in-service pavement was subjected and on determining the resulting slab behavior. A portion of State Route 22 near Murrys ville, Pennsylvania (approximately 32 km [20 miles] east of Pittsburgh) was instrumented during construction in August 2004. The instrumented section consists of 14 JPCP slabs measuring 3.7 m (12 ft) wide and 4.6 m (15 ft) long. Two types of slabs were constructed: unrestrained and restrained. The restrained slabs featured 16-mm diameter (No. 5) epoxy-coated tie bars placed every 0.8 meters (2.5 ft) along the lane/shoulder and centerline joints, and 38-mm (1.5-in) diameter epoxy-coated dowel bars placed every 305 mm (12 in) along the transverse joints. The unrestrained slabs included no tie or dowel bars.

The pavement structure comprised a 305-mm (12-in) thick PCC slab constructed on a 102-mm (4-in) asphalt treated permeable base (ATPB) layer and 127 mm (5 in) of densely graded subbase. A 610-mm (24-in) gap-graded soil and aggregate mixture was placed on top of the A-6 subgrade. Cores obtained after construction showed that the as-built thickness of the concrete slab varies between 305 mm (12 in) and 355 mm (14 in).

Thermocouples, moisture sensors and vibrating wire (VW) static strain gages were placed at various locations and depths in three restrained and three unrestrained slabs, as shown in Figure 1. Additional details concerning the construction of the test section can be found in the 2005 report by Wells et al.

3.0 Slab Curvature

As the slab is subjected to a given set of moisture and temperature gradients, slab strains vary through the thickness of the concrete, causing the slab to curl/warp either upward or downward, depending upon whether the net gradient is negative or positive. The difference in strains at the top and bottom of the slab can be used to compute the slab curvature using equation 1.

$$\rho = -\frac{\epsilon_t - \epsilon_b}{D(1 + \epsilon_t + \epsilon_b)} \quad (\text{Equation 1})$$

where: ρ = Slab curvature (positive values indicate upward curvature), in units of 1/m

ϵ_t = Strain at the top of the slab at the time of interest

ϵ_b = Strain at the bottom of the slab at the time of interest

D = Distance between the top and bottom of the slab where strain is calculated or strain measurements are taken, m.

This equation was derived using the following assumptions (Mohamed and Hansen 1997):

(a) the slab is elastic, homogenous and isotropic, with temperature-independent material properties; (b) plane sections remain plane after bending; (c) stresses and strains in the vertical direction are zero; (d) the deflection of the slab is small compared to the slab dimensions; and (e) temperature and shrinkage strains vary in the vertical direction only.

In this study, the curvatures of in-service pavement slabs were estimated or computed using calculated strains due to measured temperature and moisture conditions, actual strain measurements in the concrete slab, or pavement surface profile measurements. Each of these approaches is described in the following sections.

3.1 Curvature Estimates Based on Temperature and Moisture Measurements

Type T thermocouple wire was used to measure temperatures in the concrete and underlying layers. Sensirion SHT75 sensors were used to measure moisture and temperature variations in the concrete with a manufacturer-reported accuracy of 1.8 percent in the measured moisture content. Procedures developed by Grasley et al (2003) at the University of Illinois at Urbana-Champaign for the use of these sensors in concrete applications were followed.

Equations 2 and 3 were used to estimate the thermal and moisture strains at the slab surface as functions of the measured temperature and moisture distributions through the slab thickness, the coefficient of thermal expansion and the ultimate shrinkage strain. The required material properties were obtained through laboratory testing (Wells et al., 2005; Asbahan et al., 2006; McCracken et al., 2008). For concrete used in this test section, the

coefficient of thermal expansion was 10.6×10^{-6} mm/mm/°C (5.9×10^{-6} in/in/°F) and the ultimate shrinkage strain was 945 microstrain.

$$\varepsilon_{TempGrad} = \alpha_c \Delta T_{eq} \quad (\text{Equation 2})$$

$$\varepsilon_{MoistGrad} = -\varepsilon_{\infty} \Delta \left[1 - \frac{RH}{100} \right]_{eq}^3 \quad (\text{Equation 3})$$

where: $\varepsilon_{TempGrad}$ = thermal strain due to a temperature gradient through the slab thickness,

$\varepsilon_{MoistGrad}$ = moisture strain due to a moisture gradient through the slab thickness,

α_c = coefficient of thermal expansion of the concrete,

ε_{∞} = ultimate shrinkage strain,

ΔT_{eq} = equivalent linear temperature difference, and

$$\Delta \left[1 - \frac{RH}{100} \right]_{eq}^3 = \text{equivalent linear humidity difference coefficient.}$$

The equivalent linear temperature difference coefficient and the equivalent linear humidity difference coefficient represent the differences in temperature and moisture conditions between the top and bottom portions of the slab, with respect to the bottom of the slab. The coefficients are determined based on a regression analysis of temperature and moisture profiles. A third-degree polynomial is assumed to accurately fit the temperature and moisture profiles and the regression coefficients are used to calculate the equivalent linear difference coefficients (Jeong and Zollinger, 2005). This approach is based on a similar approach, suggested by Mohamed and Hansen (1997), to determining the linear temperature

and humidity differences through the slab based on the actual temperature and humidity differences.

The calculated strain data were zeroed based on the temperature and moisture conditions that were present at the time of set of the concrete. Early age data collected from static strain and temperature sensors in the concrete and pressure sensors along the slab/base interface were analyzed to determine the built-in gradients in the PCC slabs. The built-in temperature gradient was determined to be $0.0067^{\circ}\text{C}/\text{mm}$ ($0.31^{\circ}\text{F}/\text{in}$). Details concerning the determination of the built-in temperature gradient have been documented by Wells et al (2006). The moisture in the slab was monitored using relative humidity sensors embedded at four different slab depths. These sensors indicated that the relative humidity in the concrete remained constant at 100 percent throughout the slabs during first 24 hours after paving; this indicates that the built-in gradient due to a moisture a moisture gradient present at the time of set is not significant and can be neglected (Asbahan, 2009).

Slab curvatures computed based on the calculated thermal and moisture strains are presented in Figure 2. It is important to note that these calculated curvatures do not consider the factors that restrain slab deformation; therefore, it is likely that they overestimate the actual slab curvature. Curvature due to the calculated thermal strain fluctuates between positive and negative values throughout the two-year period, with a relatively small range of curvatures during the winter and a larger range of curvatures during other seasons. This indicates that daily fluctuations in the temperature gradient cause the slabs to curl upward and downward during all seasons at this site, and that the range of movement is smallest during the winter. The curvatures due to the calculated moisture-induced strains are mostly positive, indicating

that moisture gradients generally caused the slabs to curl upward throughout the two-year period. This is consistent with the presence of a negative moisture-induced strain gradient and an equivalent negative temperature gradient due to moisture in the slab. Soon after construction, the magnitude of the moisture-induced curvatures becomes larger than the magnitude of the thermal-induced curvatures. Therefore, the net effect is that the curvature of the slabs is predominantly upward by the summer following construction. This condition would contribute to top-down fatigue cracking (rather than the bottom-up fatigue cracking that is traditionally assumed for JPCP).

3.2 Curvature Estimates Based on Strain Measurements

Another approach to defining the shape of the slab is through strain measurements. Geokon Model 4200 Vibrating Wire (VW) concrete embedment strain gages were installed at different locations and various depths in the concrete slabs (as shown in Figure 1) to measure actual slab deformations caused by temperature changes, moisture changes and other factors that might affect slab deformation.

Raw strain readings were first corrected for the effects of temperature on the steel wire in the gage and were then converted into total strain (using Equation 4), which reflects the total deformation measured in the slab (Wells et al. 2005).

$$\epsilon_{total} = (R_t - R_0)B + (T_t - T_0)\alpha_s \quad \text{(Equation 4)}$$

where: ϵ_{total} = Total strain in the concrete (corrected for temperature effects on VW)

R_0 = Raw strain reading at time 0 (initial concrete set)

R_t = Raw strain reading at time t

T_0 = Temperature at time 0 (initial concrete set)

T_t = Temperature at time t

α_s = Thermal coefficient of expansion of steel in strain gage, $12.2 \mu\epsilon/^\circ\text{C}$ ($6.78 \mu\epsilon/^\circ\text{F}$)

B = Strain gage batch calibration factor (provided by the manufacturer)

Total measured strains calculated using equation 4 were then separated into components: strain due to temperature effects and strain due to other remaining factors (including moisture, creep, and slab restraining conditions). Strain due to uniform temperature change is estimated using equation 5 and strain due to other components is estimated by subtracting the thermal strain from the total strain, as shown in equation 6. Equation 5 does not take into account the strain induced by temperature gradients, which can be computed using Equation 2, and does not take into account the effects of slab restraint.

$$\epsilon_{TempUniform} = (T_t - T_0)\alpha_c \quad (\text{Equation 5})$$

$$\epsilon_{other} = \epsilon_{total} - (\epsilon_{TempUniform} + \epsilon_{TempGrad}) \quad (\text{Equation 6})$$

where: $\epsilon_{TempUniform}$ = Strain in the concrete due to uniform temperature change

ϵ_{other} = Strain in the concrete due to all factors that are not temperature-related

$\epsilon_{TempGrad}$ = Strain in the concrete due to equivalent linear temperature gradients, calculated in section 4.1

Slab curvatures were calculated using the strains measured along the diagonal by the static strain sensors located at the tops and bottoms of the slab corners. A summary of the history of slab curvatures computed using measured strains is presented in Figure 3. This figure

indicates that the average curvature trends were similar for the restrained and unrestrained slabs during the first two years after construction: the ranges of curvature are relatively small during the winters and larger during the summers. This is expected because the slabs are subjected to smaller temperature gradients during the winter season (resulting in smaller amounts of curvature) and larger temperature gradients during the summer (resulting in larger amounts of curvature). Computed curvatures are predominantly (>99 percent of values) positive or curled upward, which is a similar trend to that observed with the curvature calculated based on temperature and moisture measurements. This supports the theory that the slabs will be more susceptible to top-down than bottom-up cracking.

To isolate the effects of moisture, creep and slab restraint on the slabs, the curvatures calculated based on measured temperatures were subtracted from the curvatures calculated based on total strain measurements. These data are presented in

Figure 4 for both restrained and unrestrained slabs.

Figure 4 shows that the curvature influenced by moisture, creep and slab restraint generally increases throughout the two-year period, particularly for the unrestrained slabs. Since the slab restraining conditions do not change for each type of slab, the figure indicates that the moisture causes an increase in slab curvature which is counteracted by the effect of creep on the slabs. However, the overall combined effect of both factors causes an increase in the slab curvature.

3.3 Curvature Estimates Based on Surface Profile Measurements

Surface profile measurements were performed to capture changes in the slab shape under various temperature and moisture gradients. Profile measurements were accomplished using a Dipstick™, a device that provides the elevations of successive points along any surface through highly accurate measures of slope over the span of the device (FACE, 2004). Profile measurements were performed on the restrained and unrestrained slabs in the longitudinal, diagonal, and transverse directions under different temperature and moisture conditions during each season over the two-year monitoring period. By using this device several times on any given day, a dynamic representation of the surface profile variations with daily temperature gradients could be obtained.

When plotting the surface profiles, the effects of surface irregularities, built-in temperature gradients and any moisture gradients were removed from the measured profiles by subtracting from any given profile measurement another profile measurement obtained along the same profile line, on the same date, at a temperature gradient of about $0.0067\text{ }^{\circ}\text{C/mm}$ ($0.31\text{ }^{\circ}\text{F/in}$), which is the magnitude of the built-in temperature gradient. The resulting profile represents the curvature due solely to transient temperature gradient conditions.

A second-order polynomial was fitted to each zeroed and the second derivative of each polynomial was obtained to provide an estimate of the radius of curvature for each profile. The resulting data indicate that the slab surfaces are subjected to positive and negative curvatures on a daily basis, as seen in Figure 5. During the early morning hours, when temperature gradients are generally negative, the slabs tend to be curled upward; during the afternoon hours, when temperature gradients are generally positive, the slabs tend to be

curled downward. Again, the transient temperature gradients are not the actual slab curvatures that include built-in temperature and moisture effects. Therefore, they cannot be compared directly with curvatures shown in figures 2, 3 or 4.

4.0 Effect of Drying Shrinkage on Slab Curvature

A linear relationship between slab curvature and equivalent linear temperature gradient was defined using the VW data and the surface profiles by combining the curvature data with the equivalent linear temperature gradient derived from the midpanel thermocouples. Plots of curvature versus equivalent linear temperature gradient for the diagonal, longitudinal and transverse profiles of both unrestrained and restrained slabs were generated for data collected during the first three years after paving (Asbahan et al., 2006; McCracken et al., 2008), as shown in Figure 5. This represents curvature due to transient temperature gradients. This plot shows that slab curvature generally decreases as the temperature gradient in the slab increases (negative curvature values indicate downward slab curvature and positive curvature values indicate upward curvature). Figure 5 also shows that the magnitude of curvature was similar for the restrained and unrestrained slabs and ranged between 0.0003 1/m (0.0010 1/ft) and -0.0005 1/m (-0.0017 1/ft). These values are similar to the temperature measurement-based curvatures computed in section 4.1.

Figure 6 presents a plot of curvature versus equivalent linear temperature gradient data using the strain data from the restrained and unrestrained slabs for the month of April 2006 only (to limit the number of points being plotted). The month of April was selected because this month typically exhibits the widest range of temperature gradients and would, therefore,

encompass the majority of the gradients experienced throughout the year. These strains represent both built-in and transient gradients. Note that the slopes of the trendlines for the restrained and unrestrained slab data are similar, as they were in Figure 5. However, the data points in Figure 65 (based on the surface profile measurements) are essentially collinear because drying shrinkage effects have been removed, which is not the case for the data presented in Figure 6.

Figure 6 suggests that the gradients present in the restrained and unrestrained slabs when the slabs are flat (i.e., the slabs have zero curvature) are $0.0222\text{ }^{\circ}\text{C}/\text{mm}$ ($1.03^{\circ}\text{F}/\text{in}$) and $0.0407\text{ }^{\circ}\text{C}/\text{mm}$ ($1.88\text{ }^{\circ}\text{F}/\text{in}$), respectively. This is equivalent to a zero-curvature temperature difference (i.e., an effective built-in temperature difference) of $6.8\text{ }^{\circ}\text{C}$ (12.4°F) for a 305-mm (12-in) thick restrained slab and a $12.4\text{ }^{\circ}\text{C}$ (22.6°F) temperature difference for a 305-mm (12-in) unrestrained slab. The default value for effective built-in temperature difference currently suggested in the MEPDG is $5.6\text{ }^{\circ}\text{C}$ (10°F), regardless of whether the slab is doweled or undoweled. The MEPDG default value is close to that measured in this study for the restrained slab but does not appear to be appropriate for unrestrained (i.e., undoweled) slabs.

The built-in temperature gradient was previously determined to be $0.0067\text{ }^{\circ}\text{C}/\text{mm}$ ($0.31^{\circ}\text{F}/\text{in}$). The differences between this value and the effective built-in temperature gradients computed above (which include the effects of drying shrinkage and creep since construction) are $0.0016\text{ }^{\circ}\text{C}/\text{mm}$ ($0.72^{\circ}\text{F}/\text{in}$) for the restrained slabs and $0.034\text{ }^{\circ}\text{C}/\text{mm}$ ($1.57^{\circ}\text{F}/\text{in}$) for the unrestrained slabs. This restraint of free deformation results in substantially higher levels of stress. The curvatures due only to long-term drying shrinkage

and the built-in gradient (i.e., the x-axis intercepts in Figure 6) are 0.0003 1/m (0.0010 1/ft) for the restrained slabs and 0.0005 1/m (0.0017 1/ft) for the unrestrained slabs. The curvature of the restrained slabs is more than 50 percent lower than that of the unrestrained slabs.

It is somewhat surprising that the slopes of the trend lines for the restrained and unrestrained slabs are so similar. These similar slopes indicate that the rates of change in curvature with changes in the temperature gradient are similar for the restrained and unrestrained slabs. An estimate of the maximum curvature caused strictly by the temperature gradient observed throughout the month can be obtained by subtracting out the curvature due to the built-in gradient and the drying shrinkage [0.0003 1/m (0.0010 1/ft) for the restrained slab and 0.0005 1/m (0.0017 1/ft) for the unrestrained slab]. In doing this, it was found that the maximum and minimum curvatures corresponding to the minimum and maximum gradients experienced throughout the month were 0.0003 1/m (0.0010 1/ft) and -0.0006 1/m (-0.0020 1/ft), for both the restrained and unrestrained slabs. Therefore, the additional restraint provided by the dowel and tie bars does not significantly reduce slab deformations resulting from daily temperature fluctuations. These trends were also observed for the curvature values estimated from strain measurements in the longitudinal and transverse directions. Similar observations can be made using data reported previously by Vandenbossche (2003).

Plots similar to Figure 6 were made for strain data collected at various times throughout the first two years after paving. Linear regression analyses were performed so that the y-intercept could be established for each data set. The y-intercept represents the curvature in

the slab when a transient temperature gradient is not present. For the purposes of this discussion, this condition will be referred to as the “zero-gradient curvature.” The zero-gradient curvature histories were determined for the restrained and unrestrained slabs for the first two years after paving, as shown in Figure 7. These curvatures represent the effects of built-in gradients as well as drying shrinkage. Some of this drying shrinkage is reversible, as can be seen by the seasonal fluctuations. Rewetting during wet seasons (e.g., springtime) reverses a portion of the drying shrinkage and reduces the observed curvatures. The shrinkage (and, therefore, the curvature) is regained during the drier seasons. This yearly fluctuation in curvatures is about 0.0001 1/m (0.0003 1/ft) for both the restrained and unrestrained slabs.

The dowel and tie bars do not appear to have a significant effect on changes in slab curvature attributed to the seasonal fluctuations in drying shrinkage. They do, however, have a substantial effect on longer-term effects of shrinkage on observed slab curvature values. Figure 7 shows that the overall trend of the zero-gradient curvatures for the restrained slabs is relatively flat while there is an obvious increase in the zero-gradient curvature with time for the unrestrained slabs. The longer-term reduction in slab curvature for restrained slabs helps to insure the presence of more uniform support beneath the slabs and, therefore, reduces vehicle load-related stresses. These reductions in vehicle load-related stresses are at least partially offset by increases in critical slab stresses (particularly those at the top of the slab near mid-panel) due to the restraint of curvature.

5.0 Comparisons

In previous sections of this paper, slab curvature was estimated based on the calculated thermal and moisture strains, measured strains and surface profile measurements. In this section, the slab curvatures estimated using these three approaches are compared and the results are used to evaluate the effects of moisture on the drying shrinkage of the restrained and unrestrained slabs.

First, the curvatures calculated based on the VW sensors and the Dipstick data are compared. The curvatures provided in Figure 6 are estimated based on strain data collected from the VW sensors in the corner of the slab adjacent to the lane/shoulder joint and in the longitudinal, diagonal and transverse directions. The curvatures provided in Figure 5 are based on surface profiles that begin in the slab corner adjacent to the lane/shoulder joint and extend in the same three directions. The curvatures presented in Figures 5 and 6 follow the same general daily trends, with smaller curvature values resulting from estimates that are based on the measured strain data, in most cases. The trend line for the curvatures estimated from the surface profiles is shifted downward with respect to the trend line for the curvatures obtained from the strain gage data and has a flatter slope. The downward shift means that the computed curvatures under/overestimate actual total curvatures because the process of zeroing out the profile measurements removes the effects of everything except the transient temperature gradient.

Figure 8 presents comparisons of slab curvatures calculated based on temperature and moisture measurements with curvatures estimated based on strain measurements (diagonal direction only) and curvatures based on surface profile measurements (diagonal direction

only); all data presented were collected during a single day in March 2005. This figure shows that the curvatures derived from surface profile data closely fit the trend line for curvatures based on temperature measurements. Curvature due to moisture-induced strains is relatively constant throughout the test day. This confirms the previous conclusion statement that the primary difference between the curvatures computed using strain data and curvatures computed from surface profile data is due to the effects of moisture and creep.

It can also be concluded from Figure 8 that the addition of curvatures due to temperature and moisture measurements results in computed total curvatures that are larger than the curvatures estimated using strain measurements. This indicates that creep and slab restraint (in both restrained and unrestrained slabs) cause reductions in slab curvature when compared with the total curvature computed using calculated thermal and moisture gradients. For example, for the test day in March of 2005 that was used in Figure 8, unrestrained slab curvatures computed using the VW data are an average of 30 percent lower than curvatures computed using strains estimated from temperature and moisture measurements. This reduction can be attributed to the effects of slab self-weight and creep. For the restrained slabs, the average reduction is 56 percent and can be attributed to the effects of dowel bars, tie bars, slab self-weight and creep.

A comparison of the curvatures of the restrained and unrestrained slabs leads to the conclusion that the presence of dowel bars and tie bars along the joints reduced the slab curvatures by an average of 38 percent on this project. Reduced curvature affects the development of slab stresses: joint restraint increases temperature- and moisture-related

stresses (until creep and stress relaxation reduce this effect), but can reduce load-induced stresses by providing more uniform slab support. This reduction in curvature for restrained slabs was observed for all three curvature measurement/estimation techniques.

The differences between curvatures estimated using strain data and those estimated using surface profile measurements were calculated for every profile measured during every field data collection outing. Figure 9 presents a summary of the differences in curvatures for the restrained and unrestrained slabs for the two-year period following paving (using surface profiles measurements obtained along the slab diagonal). The figure shows that the calculated differences (VW-based curvature minus profile-based curvature) are positive at all times more than a few months after construction. This is consistent with the fact that curvatures based on surface profile measurements in this study represent departures from zero-gradient deformations measured on the day of testing and do not, therefore, take into account the effects of moisture-related deformations, which would otherwise increase upward (positive) slab curvature. Figure 9 also shows that the difference in curvatures varies over the two-year period, suggesting that the drying shrinkage at the slab surface is generally increasing with time as the slabs dry, but that there are seasonal fluctuations as well. Similar trends were observed for the slab curvatures measured in the longitudinal and transverse directions. Figure 9 shows that the curvature differences are smaller for the restrained slabs, confirming the previously stated finding that slab edge restraint reduces the curvature produced by moisture gradients.

Figure 9 also shows that the rate of increase in the curvature differences over time is five times larger (on average) for the unrestrained slabs than for the restrained slabs. This further illustrates the effects of slab restraint due to dowel bars on slab curvature due to drying shrinkage and supports the previously stated findings based on Figure 7.

There is significant scatter in the restrained slab curvature difference data for every test date. This scatter is most likely due to differences in the restraining conditions along the slabs. For example, it is possible that there is variability in dowel “looseness” (due to construction factors) and other restraining factors between the instrumented slabs. In addition, joint cracking patterns can affect the effective width of transverse joints (e.g., joints that crack sooner after paving are often wider than joints that crack later), which can affect the stiffness of doweled joints (i.e., reduced stiffness at wider doweled joints). This scatter in slab curvature differences was not observed for the unrestrained slabs; the unrestrained slabs exhibited a more repeatable pattern of behavior.

6.0 Summary and Conclusions

Temperature gradients in concrete slabs cause the slabs to curl upward and downward both daily and seasonally, while moisture gradients generally cause slabs to curl upward. Based on slab curvatures calculated from slab temperature and moisture measurements, it was found that slabs are predominantly curled upward within a few months after paving and they remain that way, resulting in increased potential for top-down fatigue cracking (rather than the bottom-up fatigue cracking that has traditionally been assumed in concrete pavement design). This finding was confirmed using curvatures computed from slab strain

measurements, which showed that the slabs on this project were curled upward about 99 percent of the time.

Overall curvatures in restrained slab averaged more than 60 percent lower than those of unrestrained slabs. This restraint of temperature- and moisture-related deformation can result in substantially higher levels of environmental slab stress, which decrease over time with creep and stress relaxation and may also be partially offset by reduced load-related stresses (due to more uniform support of restrained slabs).

Differences in slab curvatures estimated using static strain measurements those estimated using surface profile data can be attributed primarily to the effects of concrete drying shrinkage, which are not considered in the profile-based curvature values developed in this study. Drying shrinkage at the slab surface was observed to increase with time during the two-year period of this study, and the rate of increase in slab curvature due to drying shrinkage is larger for the unrestrained slabs than for the restrained slabs. Some of this drying shrinkage is reversible, as can be seen by the seasonal fluctuations in slab curvature, with shrinkage and slab curvature decreasing during wet seasons and increasing again during drier seasons.

The additional restraint provided by the dowel and tie bars does not appear to significantly reduce slab curvature resulting from daily temperature fluctuations or from reversible drying shrinkage. It does have a substantial effect on reducing slab curvature due to long-term drying shrinkage. This reduction in curvature help to provide more uniform support beneath

restrained slabs and, therefore, reduces vehicle load-related stresses. The restraint of slab deformation, however, does increase environmental (temperature- and moisture-related) stresses.

The 305-mm (12-in) thick slabs considered in this study were found to have effective built-in temperature differences of 6.8 °C (12.4°F) for the restrained slabs and 12.4 °C (22.6°F) for the unrestrained slabs. The default value for effective built-in temperature difference currently suggested in the MEPDG is 5.6 °C (10°F), regardless of whether the slab is doweled or undoweled. The MEPDG default value is close to that measured in this study for the restrained slab but does not appear to be appropriate for unrestrained (i.e., undoweled) slabs.

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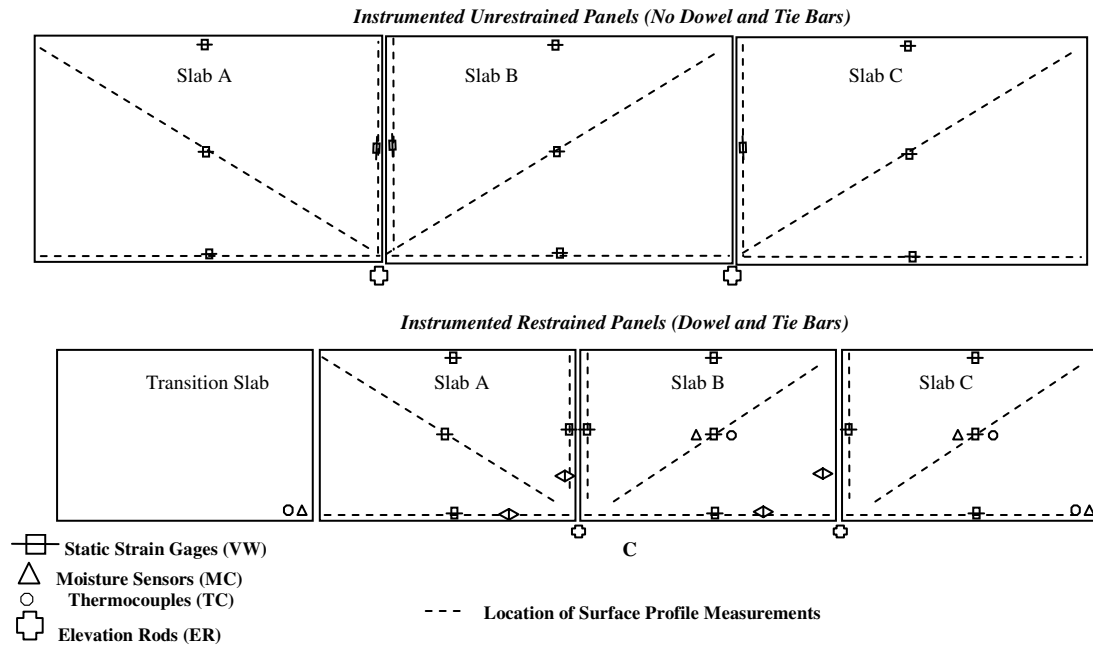


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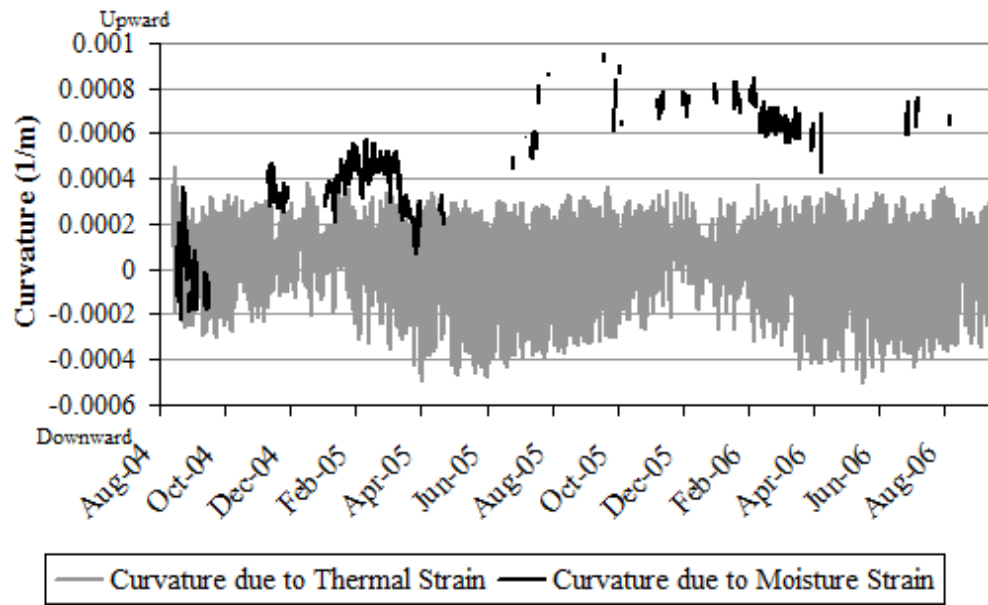


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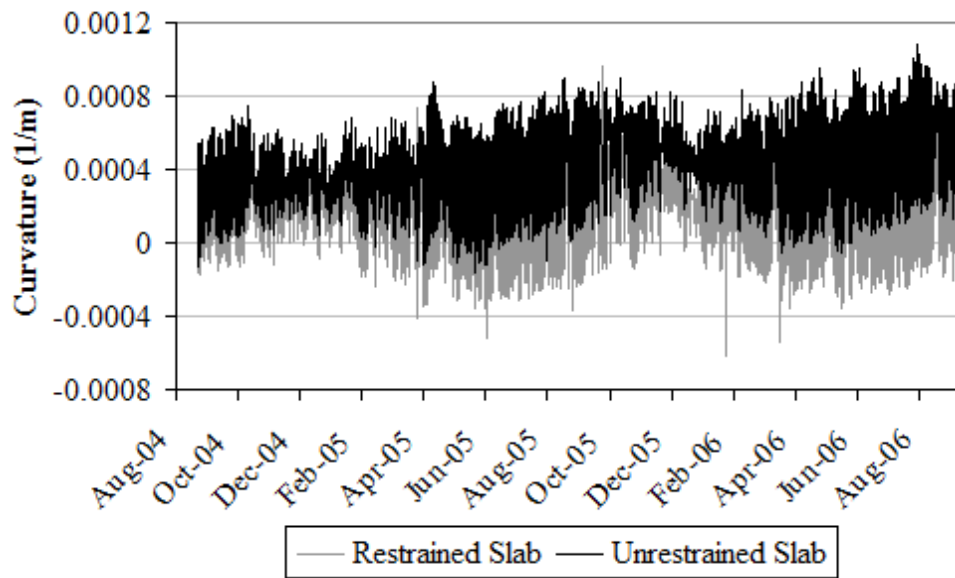


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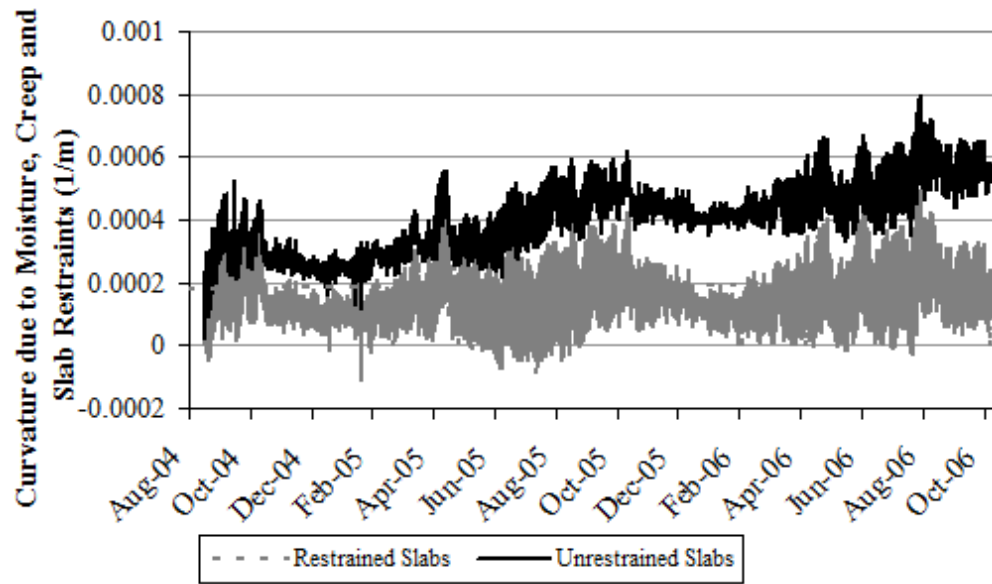


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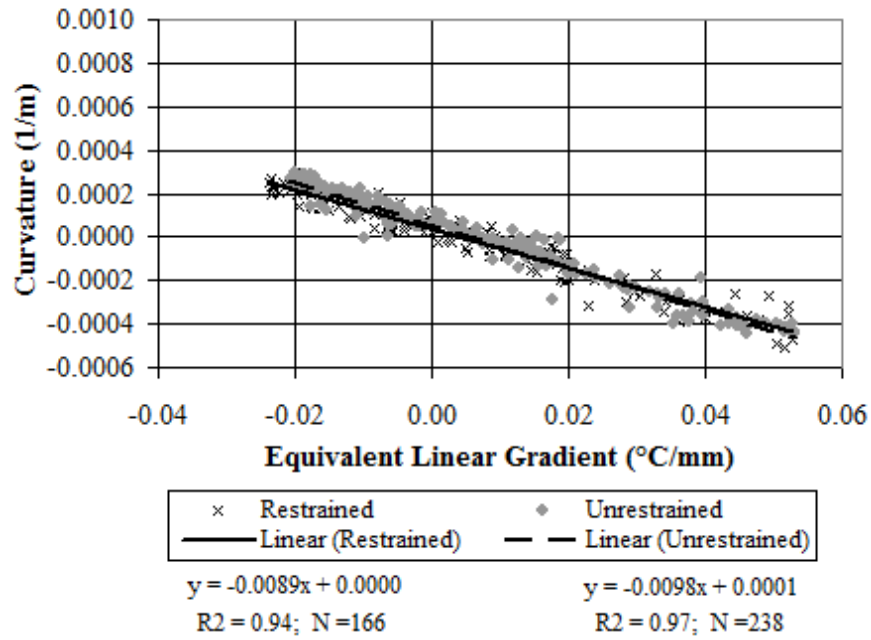


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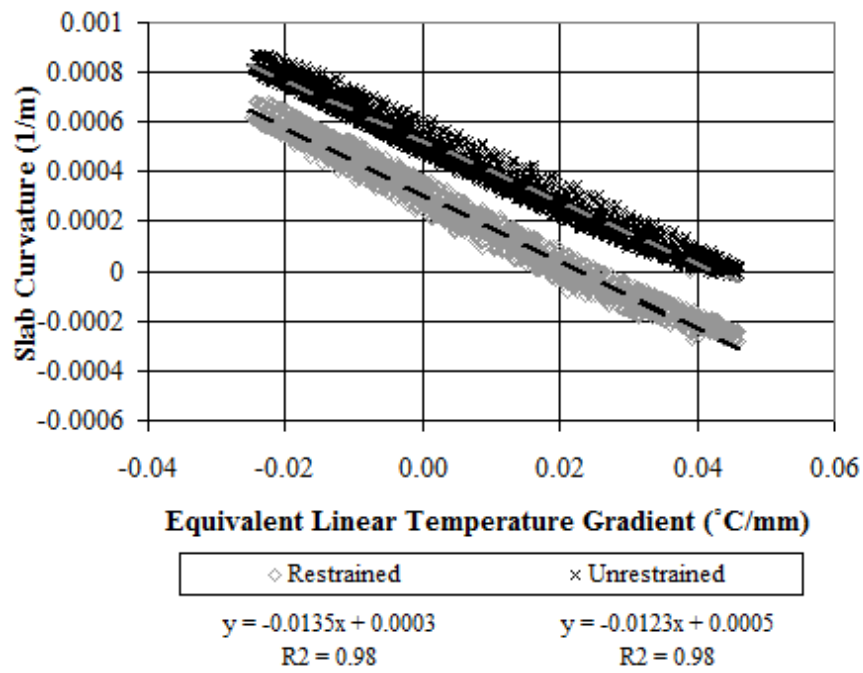


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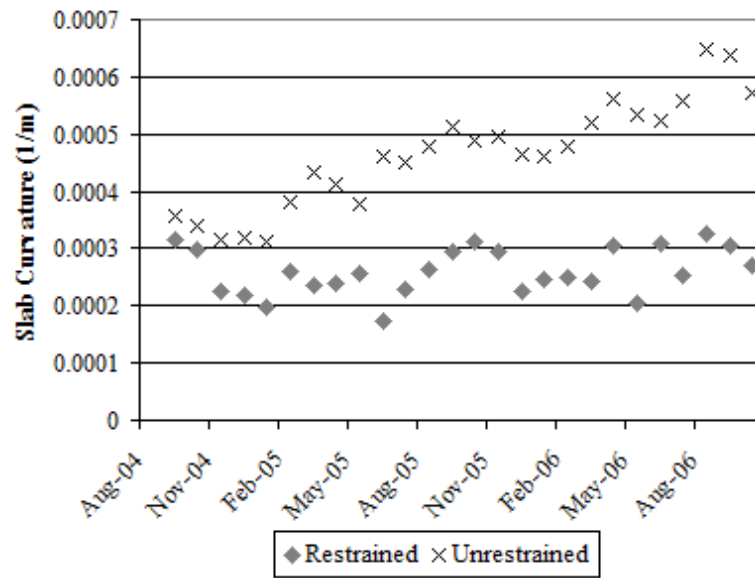


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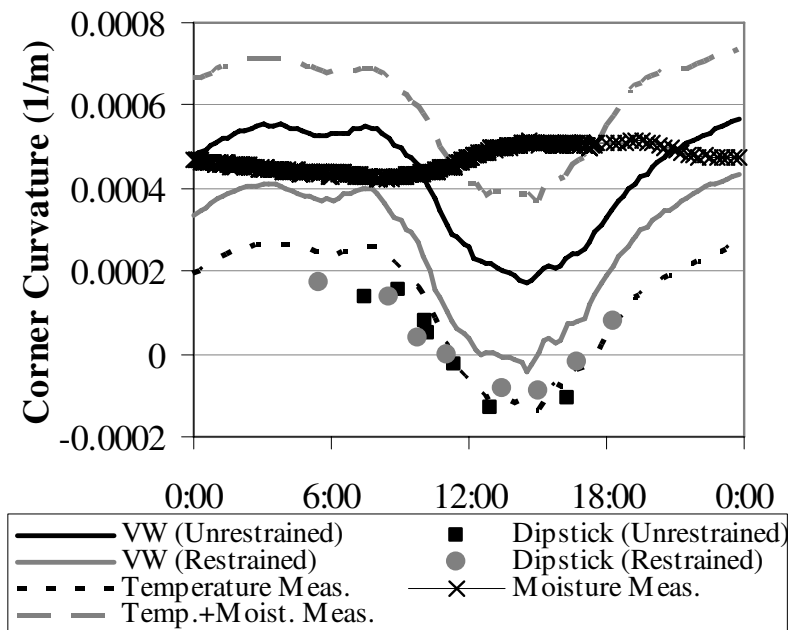


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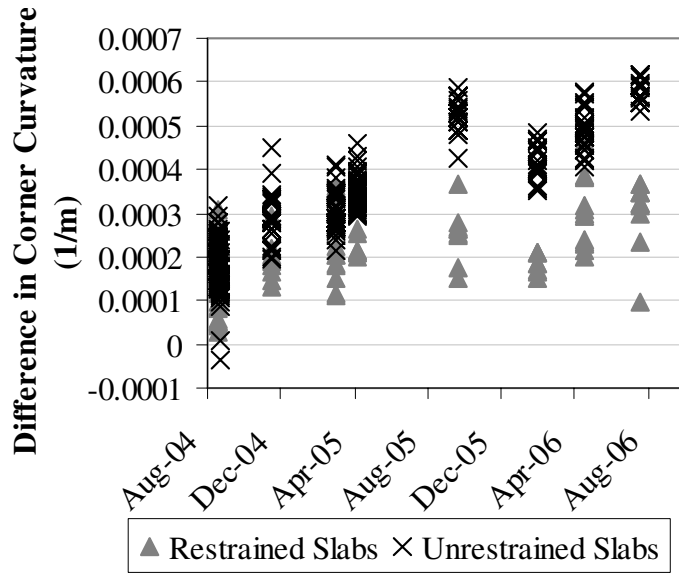


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